C.U.SHAH UNIVERSITY

Summer Examination-2017

Subject Name: Mathematics-II

Subject Code: 4SC02MAT1 Branch: B.Sc. (All)

Semester: 2 Date: 09/05/2017 Time: 02:00 To 05:00 Marks: 70 **Instructions:**

- (1) Use of Programmable calculator & any other electronic instrument is prohibited.
- (2) Instructions written on main answer book are strictly to be obeyed.
- (3) Draw neat diagrams and figures (if necessary) at right places.
- (4) Assume suitable data if needed.

Q-1 Attempt the following questions: (14)

- The solution of the differential equation $(D^2 2D + 1)y = 0$ is (01)
 - (3) $(c_1 + (c_1 + c_2))$ (4) None of these $c_1e^x+c_2e^{-x}$ (1)
- (01)
- When we put $z = \log x$ in a homogeneous linear differential equation, the value (01)
 - (1) $z^{2} \frac{d^{2}y}{dz^{2}}$ (3) $\frac{d^{2}y}{dz^{2}} \frac{dy}{dz}$ (2) $z^{2} \frac{d^{2}y}{dz^{2}} z\frac{dy}{dz}$ (4) $\frac{d^{2}y}{dz^{2}} + \frac{dy}{dz}$ The particular integral of the differential equation $(D^{2} 3D + 2)y = e^{5x}$ is (1) e^{5x} (3) 1
- (01)
 - (2)
- (01)

 - (3) $e^{-mx} \int Q \ dx$ (4) $e^{mx} \int Q \ e^{-mx} \ dx$
- The complex conjugate of $\frac{i}{1-i}$ is (01)



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(1)
                                                    (3)
      (2)
                                                    (4) None of these
                                                                                                   (01)
     Real part of \cosh z is ......
                        \cosh x \cos y
      (1)
                                                   (3)
                                                                    \cos h x \sin y
      (2)
                                                   (4)
                        sinh x sin y
                                                                     \sinh x \cos y
     If z = \cos \theta + i \sin \theta, then \sin n\theta = \dots
                                                                                                   (01)
h)
                         z^n + z^{-n}
                         \frac{z^n-z^{-n}}{2}
      (2)
                                                   (4) None of these
     If x + iy = \sqrt{2} + 3i, then x^2 + y is ......
                                                                                                   (01)
i)
                                                                          13
      (2)
                                                   (4)
                                                                       \sqrt{2} + 3
     The real part of (\sin x + i \cos x)^5 is ......
j)
                                                                                                   (01)
                          -\cos 5x
                                                                        \sin 5x
      (2)
                                                   (4)
                          -\sin 5x
                                                                        \cos 5x
     General equation to the cone which passes through the axes is .......
k)
                                                                                                   (01)
                  ax^2 + by^2 + cz^2 = 1
                                                   (3)
                                                              fyz + gzx + hxy = 1
                  ax^2 + by^2 + cz^2 = 0
                                                              fyz + gzx + hxy = 0
      (2)
                                                   (4)
l)
     The equation of the enveloping cone can be written as:
                                                                                                   (01)
                          S = T^2
                                                   (3)
                                                                        T = S_1
    (2) SS_1 = T^2 (4) Non Guiding curve of a right circular cylinder is .......
                                                   (4) None of these
                                                                                                   (01)
      (1) ellipse
                                                   (3) pair of straight lines
      (2) circle
                                                   (4) any closed curve
     The equation \frac{x^2}{2} - \frac{y^2}{3} = z represents:
                                                                                                   (01)
      (1) cylinder
                                                    (3) ellipsoid
      (2) hyperboloid
                                                         paraboloid
                                                    (4)
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Attempt any four questions from Q-2 to Q-8

Q-3

Q-2 Attempt all questions (14)(05)

Find the equation of cone whose vertex is (α, β, γ) and base $ax^2 + by^2 = 1, z = 0.$

Describe and sketch the conicoid $\frac{x^2}{9} - \frac{y^2}{16} - \frac{z^2}{9} = 1$. (05)b)

Find the equation of a cylinder whose generating lines have the direction cosine (04)(l, m, n) and which passes through the circle $x^2 + z^2 = a^2$, y = 0.

Attempt all questions (14)

Find the equation of the enveloping cylinder of the sphere $x^2 + y^2 + z^2 = 25$, (05)**a**) whose generators are parallel to the $\lim_{x \to 0} \frac{x}{1} = \frac{y}{2} = \frac{z}{3}$. Prove that the equation $2y^2 - 8yz - 4zx - 8xy + 6x - 4y - 2z + 5 = 0$

b) (05)Page 2 | | 3



		represents a cone whose vertex is $\left(-\frac{7}{6}, \frac{1}{3}, \frac{5}{6}\right)$.	
	c)	Define: $\log(x + iy)$. Determine $\log(1 - i)$.	(04)
Q-4		Attempt all questions	(14)
	a)	Prove that the n^{th} root of unity are in a geometric progression. Also show that their sum is zero.	(05)
	b)	Separate real and imaginary parts of $\tan(x-iy)$.	(05)
	c)	Solve: $y'' + 16y = x^4 + e^{3x} + \cos 3x$.	(04)
Q-5	,	Attempt all questions	(14)
	a)	Solve: $(x^2D^2 - 3xD + 4)y = x^2$, given that $y(1) = 1$ and $y'(1) = 0$.	(05)
	b)	Solve: $\frac{d^3y}{dx^3} + 2\frac{d^2y}{dx^2} + 4\frac{dy}{dx} + 8y = x^2$.	(05)
	c)	Solve: $\frac{d^2y}{dx^2} + 4\frac{dy}{dx} + 3y = e^{-3x}$.	(04)
Q-6		Attempt all questions	(14)
	a)	State and prove De-Moiver's theorem.	(05)
	b)	Prove that $\sinh^{-1}(z) = \ln(z + \sqrt{z^2 + 1})$.	(05)
	c)	Expand $\cos^5 \theta$ in a series of cosines of multiples of θ .	(04)
Q-7	,	Attempt all questions	(14)
	a)	Solve: $\frac{d^2y}{dx^2} - 3\frac{dy}{dx} + 2y = xe^{3x} + \sin 2x$.	(05)
	b)	Prove that the cones $ax^2 + by^2 + cz^2 = 0$ and $\frac{x^2}{a} + \frac{y^2}{b} + \frac{z^2}{c} = 0$ are reciprocal.	(05)
	c)	Prove that $\cos 6\theta = 32 \cos^6 \theta - 48 \cos^4 \theta + 18 \cos^2 \theta - 1$.	(04)
Q-8		Attempt all questions	(14)
	a)	Solve the simultaneous equations $\frac{dx}{dt} + 2y + \sin t = 0$, $\frac{dy}{dx} - 2x - \cos t = 0$ given	(05)
		that $x = 0$ and $y = 1$ when $t = 0$.	/A.F.
	b)	Solve: $r^3 \frac{d^3y}{d^3y} + 2r^2 \frac{d^2y}{d^3y} + 2y = 10\left(r + \frac{1}{2}\right)$	(05)





